

Georgia Standards of Excellence Curriculum Frameworks

Mathematics

GSE Fourth Grade Unit 3: Fraction Equivalents



Richard Woods, Georgia's School Superintendent "Educating Georgia's Future"

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Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Unit 3: FRACTION EQUIVALENTS

TABLE OF CONTENTS

| Overview | 3 |
|--------------------------------------|----|
| Standards for Mathematical Practice | 3 |
| Standards for Mathematical Content | 4 |
| Big Ideas | 5 |
| Essential Questions for the Unit | 5 |
| Concepts & Skills to Maintain | 5 |
| Strategies for Teaching and Learning | 6 |
| Selected Terms and Symbols | 7 |
| Tasks | 7 |
| Intervention Table | 12 |
| Formative Assessment Lessons | 13 |

Tasks-

| • | Fraction Kits | 14 |
|---|---|----|
| • | Red Rectangles | 19 |
| • | Pattern Block Puzzles | 27 |
| ٠ | Benchmark Fractions | |
| ٠ | More or Less. | 40 |
| ٠ | $\overline{\text{Close to } 0, \frac{1}{2}, \text{ or } 1}$ | 47 |
| • | Their Fair Share. | 51 |
| • | Eating Cookies | 56 |
| • | Equivalent Fractions | 64 |
| • | Making Fractions | 72 |
| • | Write About Fractions | 76 |
| • | Culminating Task: Pattern Block Puzzles Revisited | |

IF YOU HAVE NOT READ THE FOURTH GRADE CURRICULUM OVERVIEW IN ITS ENTIRETY PRIOR TO USE OF THIS UNIT, PLEASE **STOP** AND CLICK HERE: <u>https://www.georgiastandards.org/Georgia-Standards/Frameworks/4th-Math-Grade-Level-Overview.pdf</u> Return to the use of this unit once you've completed reading the Curriculum Overview. Thank you!

> Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 2 of 90 All Rights Reserved

OVERVIEW

In this unit students will:

- understand representations of simple equivalent fractions
- compare fractions with different numerators and different denominators

Although the units in this instructional framework emphasize key standards and big ideas at specific times of the year, routine topics such as estimation, mental computation, and basic computation facts should be addressed on an ongoing basis. Ideas related to the eight STANDARDS FOR MATHEMATICAL PRACTICE: making sense of problems and persevering in solving them, reasoning abstractly and quantitatively, constructing viable arguments and critiquing the reasoning of others, modeling mathematics, using appropriate tools strategically, attending to precision, looking for and making use of structure, and looking for and expressing regularity in repeated reasoning, should be addressed continually as well. The first unit should establish these routines, allowing students to gradually enhance their understanding of the concept of number and to develop computational proficiency.

These tasks are not intended to be the sole source of instruction. They are representative of the kinds of experiences students will need in order to master the content, as well as mathematical practices that lead to conceptual understanding. Teachers should NOT do every task in the unit; they should choose the tasks that fit their students' needs. The tasks in these units illustrate the types of learning activities that should be utilized from a variety of sources.

For more detailed information about unpacking the content standards, unpacking a task, math routines and rituals, maintenance activities and more, please refer to the Grade Level Overview for Grade 4.

STANDARDS FOR MATHEMATICAL PRACTICE

This section provides examples of learning experiences for this unit that support the development of the proficiencies described in the Standards for Mathematical Practice. These proficiencies correspond to those developed through the Literacy Standards. The statements provided offer a few examples of connections between the Standards for Mathematical Practice and the Content Standards of this unit. This list is not exhaustive and will hopefully prompt further reflection and discussion.

- 1. **Make sense of problems and persevere in solving them.** Students make sense of problems involving equivalent fractions and comparing fractions.
- 2. **Reason abstractly and quantitatively.** Students demonstrate abstract reasoning about relative size of fractions.
- 3. **Construct viable arguments and critique the reasoning of others.** Students construct and critique arguments regarding the equivalency of fractions.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 3 of 90 All Rights Reserved

- 4. **Model with mathematics.** Students use constructed fraction strips to demonstrate understanding of equivalent fractions.
- 5. Use appropriate tools strategically. Students select and use tools such as fraction strips and number lines to identify equivalent fractions.
- 6. Attend to precision. Students attend to the language of real-world situations to determine if one fraction is greater than another.
- 7. Look for and make use of structure. Students relate the structure of fractions to the same whole to compare fractions.
- 8. Look for and express regularity in repeated reasoning. Students relate the structure of fractions to the same whole to identify multiple equivalent fractions.

***Mathematical Practices 1 and 6 should be evident in EVERY lesson. ***

STANDARDS FOR MATHEMATICAL CONTENT

Extend understanding of fraction equivalence and ordering.

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

<u>Solve problems involving measurement and conversion of measurements from a larger unit</u> to a smaller unit.

MGSE4.MD.2 Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 4 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

BIG IDEAS

- Fractions can be represented visually and in written form.
- Fractions with differing parts can be the same size.
- Fractions of the same whole can be compared.
- Fractions with the same amount of pieces can be compared using the size of their pieces.
- Fractions can be compared using benchmarks like $0, \frac{1}{2}$ and 1.
- Fraction relationships can be expressed using the symbols, >, <, or =.

ESSENTIAL QUESTIONS Choose a few questions based on the needs of your students.

- What is a fraction and how can it be represented?
- How can equivalent fractions be identified?
- In what ways can we model equivalent fractions?
- How can identifying factors and multiples of denominators help to identify equivalent fractions?
- What are benchmark fractions?
- How are benchmark fractions helpful when comparing fractions?
- How can we use fair sharing to determine equivalent fractions?
- How do we know fractional parts are equivalent?
- What happens to the value of a fraction when the numerator and denominator are multiplied or divided by the same number?
- How are equivalent fractions related?
- How can you compare and order fractions?
- How do I compare fractions with unlike denominators?
- How do you know fractions are equivalent?
- What can you do to decide whether your answer is reasonable?
- How do we locate fractions on a number line?

CONCEPTS/SKILLS TO MAINTAIN

It is expected that students will have prior knowledge/experience related to the concepts and skills identified below. It may be necessary to pre-assess in order to determine if time needs to be spent on conceptual activities that help students develop a deeper understanding of these ideas.

- Identify and give multiple representations for the fractional parts of a whole (area model) or of a set, using halves, thirds, fourths, sixths, eighths, tenths and twelfths.
- Recognize and represent that the denominator determines the number of equally sized pieces that make up a whole.
- Recognize and represent that the numerator determines how many pieces of the whole are being referred to in the fraction.
- Compare fractions with denominators of 2, 3, 4, 6, 10, or 12 using concrete and pictorial models.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 5 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Fluency: Procedural fluency is defined as skill in carrying out procedures flexibly, accurately, efficiently, and appropriately. Fluent problem solving does not necessarily mean solving problems within a certain time limit, though there are reasonable limits on how long computation should take. Fluency is based on a deep understanding of quantity and number.

Deep Understanding: Teachers teach more than simply "how to get the answer" and instead support students' ability to access concepts from a number of perspectives. Therefore, students are able to see math as more than a set of mnemonics or discrete procedures. Students demonstrate deep conceptual understanding of foundational mathematics concepts by applying them to new situations, as well as writing and speaking about their understanding.

Memorization: The rapid recall of arithmetic facts or mathematical procedures. Memorization is often confused with fluency and automaticity. Fluency implies a much richer kind of mathematical knowledge and experience.

Number Sense: Students consider the context of a problem, look at the numbers in a problem, make a decision about which strategy would be most efficient in each particular problem. Number sense is not a deep understanding of a single strategy, but rather the ability to think flexibly between a variety of strategies in context.

Fluent students:

- flexibly use a combination of deep understanding, number sense, and memorization.
- are fluent in the necessary baseline functions in mathematics so that they are able to spend their thinking and processing time unpacking problems and making meaning from them.
- are able to articulate their reasoning.
- find solutions through a number of different paths.

For more about fluency, see: <u>http://www.youcubed.org/wp-</u> <u>content/uploads/2015/03/FluencyWithoutFear-2015.pdf</u> and: <u>https://bhi61nm2cr3mkdgk1dtaov18-wpengine.netdna-ssl.com/wp-content/uploads/nctm-timed-tests.pdf</u>

STRATEGIES FOR TEACHING AND LEARNING

- Students should be actively engaged by developing their own understanding.
- Mathematics should be represented in as many ways as possible by using graphs, tables, pictures, symbols, and words.
- Interdisciplinary and cross-curricular strategies should be used to reinforce and extend the learning activities.
- Appropriate manipulatives and technology should be used to enhance student learning.
- Students should be given opportunities to revise their work based on teacher feedback, peer feedback, and metacognition, which includes self-assessment and reflection.
- Students should write about the mathematical ideas and concepts they are learning.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 6 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

- Books such as *Fraction Action* (2007) written and illustrated by Loreen Leedy and *Working with Fractions* (2007) by David A. Adler and illustrated by Edward Miller, are useful resources to have available for students to read during the instruction of these concepts.
- Consideration of all students should be made during the planning and instruction of this unit. Teachers need to consider the following:
 - What level of support do my struggling students need in order to be successful with this unit?
 - In what way can I deepen the understanding of those students who are competent in this unit?
 - What real life connections can I make that will help my students utilize the skills practiced in this unit?

SELECTED TERMS AND SYMBOLS

Note – At the elementary level, different sources use different definitions. Please preview any website for alignment to the definitions given in the frameworks. Mathematics Standards Glossary of Mathematical Terms: <u>http://www.corestandards.org/Math/Content/mathematics-glossary/glossary</u>.

The terms below are for teacher reference only and are not to be memorized by the students.

- common fraction
- denominator
- equivalent sets
- increment
- numerator
- proper fraction
- term
- unit fraction
- whole number

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

TASKS

The following tasks represent the level of depth, rigor, and complexity expected of all fourth grade students. These tasks or tasks of similar depth and rigor should be used to demonstrate evidence of learning. It is important that all elements of a task be addressed throughout the learning process so that students understand what is expected of them. While some tasks are identified as performance tasks, they also may be used for teaching and learning.

| Scaffolding Task | Tasks that build up to the learning task. |
|-------------------|---|
| Constructing Task | Constructing understanding through deep/rich contextualized problem |
| | solving tasks. |
| Practice Task | Tasks that provide students opportunities to practice skills and |
| | concepts. |
| Performance Task | Tasks, which may be a formative or summative assessment, that check |
| | for student understanding/misunderstanding and or progress toward the |
| | standard/learning goals at different points during a unit of instruction. |
| Culminating Task | Designed to require students to use several concepts learned during the |
| | unit to answer a new or unique situation. Allows students to give |
| | evidence of their own understanding toward the mastery of the standard |
| | and requires them to extend their chain of mathematical reasoning. |
| Formative | Lessons that support teachers in formative assessment which both |
| Assessment Lesson | reveal and develop students' understanding of key mathematical ideas |
| (FAL) | and applications. These lessons enable teachers and students to |
| | monitor in more detail their progress towards the targets of the |
| | standards. |
| CTE Classroom | Designed to demonstrate how the Career and Technical Education |
| Tasks | knowledge and skills can be integrated. The tasks provide teachers with |
| | realistic applications that combine mathematics and CTE content. |
| 3-Act Task | A Three-Act Task is a whole-group mathematics task consisting of 3 |
| | distinct parts: an engaging and perplexing Act One, an information and |
| | solution seeking Act Two, and a solution discussion and solution |
| | revealing Act Three. More information along with guidelines for 3-Act |
| | Tasks may be found in the Guide to Three-Act Tasks on |
| | georgiastandards.org. |

| Task Name | Task Type/Grouping Strategy | Content Addressed | Standard(s) | Task Description |
|-----------------------|--|--|---------------------------|--|
| Fraction Kits | Scaffolding Task Individual Task | Recognize equivalent fractions | MGSE4.NF.1 MGSE4.NF.2 | Students construct a fraction kit to discuss equivalent fractions. |
| Red Rectangles | Constructing Task Individual/Partner Task | Exploring equivalent fractions through an area model | MGSE4. NF.1 MGSE4.NF.2 | Students will create rectangles using out of color tiles that meet a criteria, allowing the student to write equivalent fractions from the model. |
| Pattern Block Puzzles | Constructing Task Individual/Partner Task | Demonstrate an understanding of equivalent fractions | MGSE4.NF.1 MGSE4.NF.2 | Students will use pattern blocks to create and write equivalent fractions. |
| Benchmark Fractions | Constructing Task Small Group/Partner Task | Comparing fractions to a benchmark | MGSE4.NF.1 MGSE4.NF.2 | Students solve a problem using unit fractions to estimate about how much of a candy bar will be given to students. |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 9 of 90 All Rights Reserved

| More or Less | Practice Task Small Group/Partner Task | Comparing fractions to a benchmark | MGSE4.NF.2 | Students will use number lines to determine whether a fraction is greater than or less than a designated benchmark fraction. |
|--------------------------------|--|---|--------------------------|---|
| <u>Closest to 0, 1/2, or 1</u> | Practice Task Small Group/Partner Task | Comparing fractions | MGSE4.NF.1 MGSE4.NF.2 | Students create fractions and place them on a number line to prove they are closest to one of the benchmarks $0, \frac{1}{2}$, or 1. |
| <u>Their Fair Share</u> | Performance Task Individual Task | Recognize equivalent fractions, comparing fractions | MGSE4.NF1 MGSE4.MD.2 | Students construct an argument using equivalent fractions and comparison of fractions to determine if all students received a fair share. |
| Eating Cookies | 3 Act Task Small Group/Partner Task | Recognize equivalent fractions | MGSE4.NF.1 MGSE4.NF.2 | Students develop questions about fractions based on a video of children sharing cookies. Students then investigate and develop a solution for the question. |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 10 of 90 All Rights Reserved

| Equivalent Fractions | Practice Task Individual/Partner Task | Using multiplicative/finding equivalent fractions | MGSE4.NF.1 MGSE4.NF.2 | Students make equivalent fractions by slicing models and writing equation using multiplication and division by a fraction equivalent to one. |
|------------------------------------|---|---|--------------------------|---|
| Making Fractions | Practice Task Partner Task | Compare and order fractions | MGSE4.NF.2 | Students use a deck of cards to make fractions. Students compare the fractions to find which is the greatest. |
| Write About Fractions | Performance Task Small Group/Partner Task | Write fraction number sentences and explain equivalence | MGSE4.NF.1 MGSE4.NF.2 | I think this task should be moved to Unit 4. It would be a good way to start the unit on adding fractions. |
| Pattern Block Puzzles Revisited | Culminating Task Individual Task | Write fraction number sentences, identify and represent equivalence | MGSE4.NF.1 MGSE4.NF.2 | Students cover designs with pattern blocks to determine the fractional value of each pattern block being used. |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 11 of 90 All Rights Reserved

INTERVENTION TABLE

The Intervention Table below provides links to interventions specific to this unit. The interventions support students and teachers in filling foundational gaps revealed as students work through the unit. All listed interventions are from New Zealand's Numeracy Project.

| Cluster of Standards | Name of Intervention | Snapshot of summary or Student I can statement | Materials Master | | |
|----------------------------------|---|---|------------------|--|--|
| | Creating Fractions | Find simple fractions of regions. | | | |
| | | Identify the symbols for halves, quarters, thirds, fifths, and | | | |
| Extend understanding of fraction | Non-unit Fractions | Non-unit Fractions tenths including fractions greater than 1. | | | |
| equivalence and ordering. | | Find equivalent fractions and order fractions. | | | |
| MGSE4.NF.1 | Fraction Circles Order fractions with the same denominator. | | | | |
| MGSE4.NF.2 | Ordering Fractions | Order fractions with like denominators. | | | |
| | Who Has More Cake? | Order unit fractions. Find equivalent fractions and order fractions. | | | |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 12 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

FORMATIVE ASSESSMENT LESSONS (FALS)

Formative Assessment Lessons are designed for teachers to use in order to target specific strengths and weaknesses in their students' mathematical thinking in different areas. A Formative Assessment Lesson (FAL) includes a short task that is designed to target mathematical areas specific to a range of tasks from the unit. Teachers should give the task in advance of the delineated tasks and the teacher should use the information from the assessment task to differentiate the material to fit the needs of the students. The initial task should not be graded. It is to be used to guide instruction.

Teachers may use the following Formative Assessment Lessons (FALS) Chart to help them determine the areas of strengths and weaknesses of their students in particular areas within the unit.

| Formative Assessments | FALS (Supporting Lesson Included) | Content Addressed | Pacing (Use before and after these tasks) |
|--------------------------|--|----------------------|--|
| Picking Fractions | | Equivalent Fractions | Fraction Kits Write about Fractions More or Less Closest to 0, ½, 1 Equivalent Fractions |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 13 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Scaffolding Task: Fraction Kits

Back to Task Table

Inspired by Math Solutions Publications Teaching Arithmetic: Lessons for Introducing Fractions by Marilyn Burns

TASK CONTENT: In this task, students construct their own set of fraction strips.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b}$ ex: $\frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICES TO BE EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Constructing the idea that fractions are relationships, and that the size or amount of the whole matters, is a critical step in understanding fractions. Fair sharing contexts also provide learners with opportunities to explore how fractional parts can be equivalent without necessarily being congruent. They may look different but still be the same amount. Students have worked with the concept of fair share or partitioning beginning in 2nd grade, with standards that refer to same-sized shares or equal shares. Students should have knowledge of vocabulary terms such as *numerator and denominator*.

Some common misconceptions, found in Math Misconceptions, that children have include:

• Dividing nontraditional shapes into thirds, such as triangles, is the same as dividing a rectangle into thirds. If they are only used to dividing traditional shapes – circles, squares, and rectangles – they begin to think that all shapes are divided similarly.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 14 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

• Children often do not recognize groups of objects as a whole unit. Instead they will incorrectly identify the objects. For example, there may be 2 cars and 4 trucks in a set of 6 vehicles. The student may mistakenly confuse the set of cars as 2/4 of the unit instead of 2/6 or 1/3 (Bamberger, Oberdorf, & Schultz-Ferrell, 2010).

Therefore, it is important that students are exposed to multiple units of measure, various shapes, and denominators other than halves, thirds, and fourths. Additionally, the denominator used as an expression of the whole is a key concept to express for mastery.

ESSENTIAL QUESTIONS

• How can equivalent fractions be identified?

MATERIALS

• Construction paper strips of equal length (8 different colors prepared prior to beginning task with students)

GROUPING

Individual

NUMBER TALKS

Number Talks should now be firmly established as part of the daily math routine. Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" that could be included in a number talk to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents*, 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

Comments: Be sure to cut the strips of construction paper accurately before asking students to make kits. Students should create their own kits since there are basic concepts about fractions to be learned from the process of creating the kit. It is important to discuss the concept of fair sharing. Ask them how they would share the strips of colored paper among various groups of people (two, three, four, six, eight, and sixteen). It is important that you allow time for students to determine the appropriate way to equally share the strips of paper among the various groups. For students who are unable to determine the appropriate measures, ensure they are exposed to strategies discovered by their peers through classroom discussions.

• To cut fourths, first have students cut halves, then fold and cut each half into fourths.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 15 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

- To cut eighths, first have students cut fourths (as above), then cut each fourth in half to make eighths.
- To cut sixteenths, have students cut eighths (as above), then cut each eighth in half to make sixteenths.
- To cut thirds, use the concept of measurement. Tell students that the strip is 18 inches long. How many inches should each piece be if we want thirds, or three equal pieces? Students should have time for small group discussion and sharing.
- To cut sixths, follow the same idea as with thirds, but pose cutting the 18inches into six equal sized pieces. Again, students should have time for small group discussion and sharing.

This task is one that enables the construction of a manipulative that can be used with subsequent tasks. It is also important for students to have a concrete experience to draw from in the future as they move to a more abstract thinking of equivalent fractions in fifth grade. Therefore, it is important that all students are provided with an opportunity to construct their own fraction kit.

Task Directions:

Cut 12-by-18-inch construction paper lengthwise into 3-by-18-inch strips. For the fractions 1 whole, $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$, and $\frac{1}{16}$, you will need 5 different colors. To include $\frac{1}{3}$, $\frac{1}{6}$, and $\frac{1}{12}$, you will need an additional 3 colors (for a total of 8 colors.)

- Ask students to take a strip of a particular color (that you choose or the class agrees upon), fold it in half, and cut it into two pieces. Have them label each piece $\frac{1}{2}$ (and possibly also with the name 'one half') and discuss why this label is appropriate (because the pieces are the same size, each is one of the two pieces, which we represent as $\frac{1}{2}$).
- Choose a color for a second strip and have the students fold and cut it into four equal pieces. Instruct students to label each piece ¹/₄ (and possibly with the name 'one fourth'). Have students explain why the label is appropriate.
- Have students fold, cut, and label a third strip in eighths and a fourth strip in sixteenths. (For the sixteenths, students may need to fold a strip in half, cut it, and then fold each half into eighths.)
- Students leave one of the strips whole and label it 1 or 1/1 (ask students first what they should label it).
- For creating thirds, students would probably be inaccurate in folding. One strategy is to measure the strip, divide the length into three equal segments, and then measure and cut and label.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 16 of 90 All Rights Reserved

- To cut sixths, follow the same idea as with thirds, but pose cutting the 18 inches into six equal sized pieces. Again, students should have time for small group discussion and sharing.
- To cut twelfths, follow the same idea as with thirds and sixths, but pose cutting the 18 inches into 12 equal sized pieces. Again, students should have time for small group discussion and sharing.

After making the kit, have students to get out a piece that has a size of $\frac{1}{2}$. Then, ask students if they can use fraction pieces that are a different size to make a piece that is the same size as the $\frac{1}{2}$ piece. Allow students to experiment with the pieces and see that they can use two $\frac{1}{4}$ pieces to make $\frac{2}{4}$, four $\frac{1}{8}$ pieces to make $\frac{4}{8}$, three $\frac{1}{6}$ pieces to make $\frac{3}{6}$ or six $\frac{1}{12}$ pieces to make $\frac{6}{12}$. All of these fractions are the same size, or equivalent to $\frac{1}{2}$. Writing the statement $\frac{1}{2} = \frac{2}{4} = \frac{4}{8} = \frac{3}{6} = \frac{6}{12}$ will allow students to see numerically the relationship between the fractions. They may suggest patterns that they see, suggest other fractions that could be included in the statement or make the connection that any fraction is equivalent to one half if the denominator is double the numerator. Students may also make connections that all the denominators are multiples of two.

 $\frac{1}{8}$ and discussing what patterns students see as they write equivalency statements.

FORMATIVE ASSESSMENT QUESTIONS

- What was the initial cut you made to your colored strips? Why?
- Are your labels appropriate? Why or why not? How do you know?
- Could you use the strips for halves or fourths as a template for making thirds or sixths? Why or why not?
- Which fraction piece is bigger, $\frac{1}{2}$ or $\frac{1}{4}$? Next, $\frac{1}{3}$ or $\frac{1}{6}$?

DIFFERENTIATION

Extension

• Ask students to explain why making other fractions such as $\frac{1}{7}$ would be difficult. Can you name other fractions that would be difficult? How would you go about making them?

Intervention

- Begin by having students work only with halves, thirds, and fourths only.
- Discuss how these pieces compare to the whole.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 17 of 90 All Rights Reserved Intervention Table

TECHNOLOGY

- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L540</u> Making and Investigating Fraction Strips: This lesson has students make and use a set of fraction strips. It can be used for remediation purposes.
- <u>http://www.eastsideliteracy.org/tutorsupport/documents/HO_Fractions.pdf</u> Student Handout - Fraction Kit: This document provides a template for a fraction kit. It can be used with this task or for remediation purposes.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 18 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Constructing Task: Red Rectangles

Back to Task Table

(Adapted from ETA Cuisenaire's Super Source activity entitled Building Rectangles)

TASK CONTENT: For this activity students are asked to build several rectangles that are colored red over the same proportional area.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b}$ ex: $\frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

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- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning

BACKGROUND KNOWLEDGE

Before asking students to work on this task, be sure students are able to:

- Recognize that fractions are equivalent if they are the same size or if they are at the same point on a number line.
- Represent unit fractions and non-unit fractions on a number line.
- Understand that a fraction is quantity formed when something is partitioned in to equal sized pieces.

ESSENTIAL QUESTIONS

- How can we find equivalent fractions?
- In what ways can we model equivalent fractions?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 19 of 90 All Rights Reserved Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

• How can identifying factors and multiples of denominators help to identify equivalent fractions?

MATERIALS

- Color Tiles
- "Red Rectangles" student recording sheet
- Die cut color tiles or pencils and crayons for recording findings

GROUPING

Individual or partner

NUMBER TALK

Continue utilizing the different strategies in number talks and revisiting based on the needs of your students.

Students can once again utilize the friendly number strategies to begin discussing multiples and specifically combining multiples to arrive at a larger product. For example, students could solve the following string of numbers:

1 x 12 = 12

2 x 12 = 24

by combining the products of 12 and 24 as well as combining the factors of 1 and 2 the students will produce another multiple of 12, namely $3 \times 12 = 36$

$$\begin{array}{r}
1 x 12 = 12 \\
+ 2 x 12 = 24 \\
\hline
3 x 12 = 36
\end{array}$$

Doubling and halving will also help students build equivalent fractions. (Number Talks, 2010, Sherry Parrish).

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments: For this activity students are asked to build several rectangles that are colored red over the same proportional area. However, each rectangle has to be a different, namely larger, size. Students will need a number or red color tiles but also, they will need other colors as well. They will have to build several rectangles. They can do this with as much creativity as they choose using the given proportions.

The following example can be utilized as a mini lesson or students could discover this on their own. Ask students to build a rectangle that is $\frac{1}{4}$ red. Students can approach the task in several ways.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 20 of 90 All Rights Reserved



All three of these rectangles are a different size, however they all contain the same proportion of red tiles. Each is $\frac{1}{4}$ red however a different number of tiles make up that proportion of $\frac{1}{4}$. Students are then asked to write an equivalency statement similar to the one below, as well as record their work on graph paper:

 $1/_4 = 2/_8 = 3/_{12}$

This is an excellent opportunity to discuss the importance of equivalency as it relates to the same-sized whole. These fractions are proportionally equivalent in relationship to these models, but they do not reference the same sized whole. Are they truly equal?

If available, students can glue die-cut color tiles. Students can also make a representation of their rectangles using colored pencils and grid paper. Additionally, this task could be introduced by reading *The Hershey's Milk Chocolate Bar Fractions Book*, by Jerry Pallotta, illustrated by Rob Bolster or another story about equivalent fractions.

Task Directions:

How can you use Color Tiles to show fractional parts of different rectangles?

• Working with a partner, use Color Tiles to build at least 3 different-sized rectangles to represent each of these situations:

 $\frac{5}{6}$ of the tiles are red $\frac{2}{3}$ of the tiles are red $\frac{3}{4}$ of the tiles are red $\frac{2}{5}$ of the tiles are red Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents

athematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 21 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

- Record your solutions. For each rectangle, write both the total number of tiles and the number of tiles that are red.
- Be ready to talk about how you know your solutions are correct.

FORMATIVE ASSESSMENT QUESTIONS

- How are you keeping your work organized?
- How do you know these two fractions are equivalent?
- How many different illustrations can be created to show equivalent fractions? How do you know?
- How did you go about deciding how many tiles should be in each rectangle?
- How did you figure out how many red tiles to use?
- How did you find a second solution for each situation?
- How do the numbers in the fraction relate to the different tiles you used to create your rectangles?
- Look at the posted solutions. Are there any that you think are not correct? If so, tell why.
- Do you think that there are other solutions beyond those posted? Explain.
- How is it possible that there could be more than one solution for each situation?

DIFFERENTIATION

Extension

- Students could explore denominators other than those listed in the standard, such as 9, 15, 24, etc.
- Students could experiment with only two colors and begin to make discoveries about what the remaining fraction may be. For example, if $\frac{1}{4}$ of our tiles are red the remaining blue tiles must be $\frac{3}{4}$.
- Students could also make very large rectangles of up to 100 and begin to discover some of the friendly equivalent fractions for hundredths like $\frac{1}{5}$, $\frac{1}{10}$ and $\frac{1}{2}$.
- Students could continue far beyond 3 or more rectangles and challenge one another to find as many as possible, which could lead to a discussion of whether there are a finite number of ways to represent a fraction.

Intervention

- Allow students to begin by representing rectangles that are ¹/₂ red prior to exploring other fractions.
- Cutting out strips of inch graph paper would also allow students to fold and manipulate the rectangles into fourths. For example, if you cut out a strip of 8 squares on graph paper and had students fold in half twice, they would see that they now have four parts with 2 squares in each part.

Folds

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 22 of 90 All Rights Reserved

Intervention Table

TECHNOLOGY

• <u>http://illuminations.nctm.org/ActivityDetail.aspx?ID=80</u> Equivalent Fractions: This lesson involves creating equivalent fractions by dividing and shading squares or circles. It can be used for additional practice or remediation purposes.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 23 of 90 All Rights Reserved

Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

Name _____ Date _____

Red Rectangles

How can you use Color Tiles to show fractional parts of different rectangles?

PART 1

Working with a partner, use Color Tiles to build at least 3 different-sized rectangles to represent each of these situations:

| $\frac{5}{6}$ of the tiles are red | $\frac{2}{3}$ of the tiles are red |
|------------------------------------|------------------------------------|
| $\frac{3}{4}$ of the tiles are red | $\frac{2}{5}$ of the tiles are red |

Record your solutions. For each rectangle, write both the total number of tiles and the number of tiles that are red.

Be ready to talk about how you know your solutions are correct.

PART 2

Write several of your equivalent fraction in the spaces provided below:



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 24 of 90 All Rights Reserved

Georgia Department of Education Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

Describe any patterns you see in the numerators and/or denominators:

Describe some ways that you could create an equivalent fraction:

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 25 of 90 All Rights Reserved

Georgia Department of Education Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

1 inch graph paper

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 26 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

COL I rachen Equivalent

Constructing Task: Pattern Block Puzzles

Back to Task Table

TASK CONTENT: Students will make equivalent fractions using pattern blocks.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE TO BE EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.

BACKGROUND KNOWLEDGE

Before asking students to work on this task, be sure students are able to:

- Recognize that fractions are equivalent if they are the same size or if they are at the same point on a number line.
- Represent unit fractions and non-unit fractions on a number line.
- Understand that a fraction is quantity formed when something is partitioned in to equal sized pieces.

ESSENTIAL QUESTIONS

- How can we find equivalent fractions?
- In what ways can we model equivalent fractions?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 27 of 90 All Rights Reserved Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

MATERIALS

- Pattern blocks
- "Pattern Block Puzzles" student recording sheet
- Die cut paper pattern blocks (or pencils and crayons for recording findings)
- "Pattern Block Puzzles, Version 2" student recording sheet, for intervention students only

GROUPING

Individual or partner

NUMBER TALK

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" that could be included in a number talks to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents*, 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

Students can once again utilize the friendly number strategies to begin discussing multiples and specifically combining multiples to arrive at a larger product. For example, students could solve the following string of numbers:

 $1 \ge 12 = 12$ $2 \ge 12 = 24$

by combining the products of 12 and 24 as well as combining the factors of 1 and 2 the students will produce another multiple of 12, namely $3 \times 12 = 36$.

| | 1 x 12 = 12 |
|---|-----------------|
| + | 2 x 12 = 24 |
| | $3 \ge 12 = 36$ |

Doubling and halving will also help students build equivalent fractions. (Number Talks, 2010, Sherry Parrish).

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments

A limited set of pattern blocks should be available for the students. It may be helpful to create sets of pattern blocks in plastic bags beforehand for ease in distributing them to the student groups. One possible "limited set" of pattern blocks might have 1 hexagon, 1 trapezoid, 1 rhombus, and 3 triangles. This set would require students to apply their understanding of equivalent fractions as developed in this unit.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 28 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

If available, students can glue die-cut pattern block pieces. Alternately, students can manipulate the virtual pattern blocks online and easily print and then label their work. One site for pattern blocks is: <u>http://gingerbooth.com/flash/patblocks/patblocks.php</u>.

This task could be introduced by reading *The Hershey's Milk Chocolate Bar Fractions Book*, by Jerry Pallotta, illustrated by Rob Bolster or another story about equivalent fractions.

Task Directions:

Students will follow directions below from the "Pattern Block Puzzle" student recording sheet.

- Obtain a set of pattern blocks.
- Use the pattern blocks to show equivalent fractional amounts.
- Record the equivalent fractions on the "one whole" pairs below.
- Write a number sentence for each equivalent fraction. (See example.)
- How many equivalent fractions can you find?
- Use what you know about factors and multiples to identify two equivalent fractions without using the pattern blocks.
- Of the fractions that are equivalent, which one uses the least number of pattern blocks?

Example:



Encourage students to organize their thinking to be sure they have found as many ways as possible to represent equivalent fractions. Listed below are all of the possible equivalent fractions that are possible with this pattern block activity. After this task, students should be able to:

- identify the number of equal pieces needed to cover one whole as the denominator
- show equivalent fractions with the pattern blocks
- record on the student sheet equivalent fractions (either by coloring or gluing die cut pattern blocks)
- write an equation which shows the equivalent fractions

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 29 of 90 All Rights Reserved

Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3



FORMATIVE ASSESSMENT QUESTIONS

- How are you keeping your work organized?
- Have you found all of the possible equivalent fractions? How do you know?
- How do you know these two fractions are equivalent?
- How many different illustrations can be created to show equivalent fractions? How do you know?

DIFFERENTIATION

Extension

• Use a hexagon and rhombus to represent one whole or use a hexagon and a trapezoid to represent one whole.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 30 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

• How could you show one-third of this figure? (See diagram below.) Students will need to create a "new" pattern block made from two rhombi to show one-third. Students could then be asked to find equivalent fractions for thirds.



• Encourage students to add some of the fractions found in this task. This will give students an opportunity to begin exploring fractions greater than one and mixed numbers. Be sure pattern block models are used to show the addition problems.

Intervention

• Allow students to use the "Pattern Block Puzzles, Version 2" student recording sheet. In version 2, the whole is represented by the yellow hexagon. Students should be able to find most if not all of the possible equivalent fractions.

Intervention Table

TECHNOLOGY

- <u>https://prod.classflow.com/classflow/#!/product/itemId=91d03de3f5e14311b07ed97489e</u> <u>e87d4</u> This lesson can be used with an ActivSlate or Smartboard. It can be used as a mini-lesson to introduce the task or for remediation purposes.
- <u>https://learnzillion.com/lesson_plans/323</u> LearnZillion Lesson Plan: Generate Equivalent Fractions by Using Fraction Strips This lesson plans provides a real-world problem that could help students apply knowledge of equivalent fractions.
- <u>http://www.mathlearningcenter.org/web-apps/pattern-shapes/</u> *This tool provides the opportunity for students to virtually manipulate pattern blocks.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Name _____

_____Date _____

Pattern Block Puzzles

Directions:

- Obtain a set of pattern blocks from your teacher.
- Use the pattern blocks to show equivalent fractional amounts.
- Record the equivalent fractions on the "one whole" pairs below.
- Write a number sentence for each equivalent fraction. (See example.)
- How many equivalent fractions can you find?
 - Use what you know about factors and multiples to identify two equivalent fractions without using the pattern blocks.
 - Of the fractions that are equivalent, which one uses the least number of pattern blocks?



Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Name _____

_____ Date _____

Pattern Block Puzzles Version 2

Directions:

- Obtain a set of pattern blocks.
- Use the pattern blocks to show equivalent fractional amounts.
- Record the equivalent fractions on the "one whole" pairs below.
- Write a number sentence for each equivalent fraction. (See example.)
- How many equivalent fractions can you find?
 - Use what you know about factors and multiples to identify two equivalent fractions without using the pattern blocks.
 - Of the fractions that are equivalent, which one uses the least number of pattern blocks?



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 33 of 90 All Rights Reserved



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 34 of 90 All Rights Reserved



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 35 of 90 All Rights Reserved



Back to Task Table

Constructing Task: Benchmark Fractions

Adapted from Fosnot, C. The Field Trip, Context for Learning Mathematics.

TASK CONTENT: The main focus of this task is on the development of reasonableness of judging the magnitude of fractional amounts.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE TO BE EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Students were familiarized with the benchmark fraction $\frac{1}{2}$ in 2nd grade. They worked to partition circles and rectangles into halves and thirds. In 3rd grade students generated simple equivalent fractions and were required to explain why the fractions were equivalent.

ESSENTIAL QUESTIONS

• How can benchmark fractions be used to compare fractions?

MATERIALS

- Connecting cubes
- Strips of equal length paper
- Fraction Kits

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 36 of 90 All Rights Reserved
Georgia Department of Education Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

GROUPING

Small group or partner

NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. In addition Catherine Fosnot has developed problem "strings" which may be included in number talks to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents*, 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments

For this task, if some students immediately say $\frac{17}{22}$, having constructed the idea of fractions as fair sharing division from previous tasks, acknowledge their thinking but explain you were wondering about how much that would be. In a real situation, no one is going to cut a candy bar into 22 pieces, and you are wondering about how much that amount is so that the fewest possible cuts could be made. Direct students to the guiding questions listed on their student sheet. The main focus of this task is on the development of reasonableness of judging the magnitude of fractional amounts.

Task directions:

Students will follow the directions below from the "Benchmark Fractions" task sheet.

Mr. Toms' 4th grade class just concluded a unit on the solar system. To celebrate how hard students worked, Mr. Toms decided to purchase Milky Way candy bars for students to share. The grocery store only had 17 of the king size candy bars, but there are 22 students in his class. If Mr. Toms buys the bars, about how much of a bar would each student receive? Is the amount about $\frac{1}{2}$, $\frac{1}{4}$, $\frac{3}{4}$, $\frac{2}{3}$ or 1 whole? Where could one cut be made that would be a nice approximate?

FORMATIVE ASSESSMENT QUESTIONS

- What do you notice about the unit fractions you have created?
- If you tried dividing, would you have the same results?
- What is the estimated size of the fraction you created with that cut?
- What you are doing with the pieces of the bars as you work with them?
- Does your answer make sense? How do you know?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 37 of 90 All Rights Reserved

DIFFERENTIATION

Extension

• Explain how the process for redistributing the pieces differs as the number of candy bars and/or number of students changes.

Intervention.

• Students can cut out drawings of the bars, then cut off pieces and move them to make approximate equivalent amounts.

Intervention Table

TECHNOLOGY

- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L541</u> More Fun with Fraction Strips: This lesson has students work with fraction strips to compare and order fractions using relationships. It can be used for additional practice, remediation or extending understanding of the concept.
- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L347</u> Exploring the Value of the Whole: This lesson has students consider the size or value of the same fraction when different wholes are compared. It can be used for remediation purposes, additional practice, and/or extending understanding of the concept.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Name _____

Date

Benchmark Fractions



Mr. Toms' 4th grade class just concluded a unit on the solar system. To celebrate how hard students worked, Mr. Toms decided to purchase Milky Way candy bars for students to share. The grocery store only had 17 of the king size candy bars, but there are 22 students in his class. If Mr. Toms buys the bars, about how much of a bar would each student receive?

Is the amount about $\frac{1}{2}$, $\frac{1}{4}$, $\frac{3}{4}$, $\frac{2}{3}$ or 1 whole?

Where could one cut be made that would be a nice approximate?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 39 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Practice Task: More or Less

Back to Task Table

Adapted from Actions on Fractions, Navigating through Number and Operations in Grades3-5.

TASK CONTENT: In this task, students will practice compare fractions to a given amount.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICES TO BE EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.

BACKGROUND KNOWLEDGE

Students were familiarized with benchmark fraction $\frac{1}{2}$ in 2nd grade. They worked to partition circles and rectangles into halves and thirds. In 3rd grade students generated simple equivalent fractions and were required to explain why the fractions were equivalent.

ESSENTIAL QUESTIONS

- What are benchmark fractions?
- How are benchmark fractions helpful when comparing fractions?

MATERIALS

• More or Less game cards

GROUPING

Small group or partner

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 40 of 90 All Rights Reserved

NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" which may be included in number talks to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents,* 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard) Also, students can continue to explore area models and partial products to improve their ability to find equivalent fractions and skip county by any number. See page 247 in *Number Talks* (Number Talks, 2010, Sherry Parrish).

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments

Review the meaning of fraction and the ways in which the students can compare two fractions. Explore the patterns that the students have discovered for determining the greatest or least fractions. Help students think about fractions in four groups: fractions with the same denominators, fractions with a numerator of 1, fractions with same numerators (other than 1), and fractions with different numerators and different denominators.

Discuss placing fractions on a number line separated into equal parts. It is important to maintain the idea of comparing fractions using the same whole. 3



Task directions:

Students will follow the directions below from the "More or Less" student sheet.

Round 1: Benchmark fraction is $\frac{3}{4}$

- 1. Pull a card from the top of the stack.
- 2. Determine if the fraction is greater or less than $\frac{3}{4}$. Explain to your partner(s) why you believe it is greater or less.
- 3. For the other player(s), think of another way to explain why the fraction is more or less and share with the group.
- 4. Pull another card and complete steps 2-3 until all cards have been used.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 41 of 90 All Rights Reserved Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Round 2: Benchmark fraction $\frac{1}{2}$

- 1. Pull a card from the top of the stack.
- 2. Identify an equivalent fraction for the benchmark fraction.
- 3. Determine if the fraction is larger or smaller than $\frac{1}{2}$. Explain to your partner(s) why you believe it is greater than or less than using a number line.
- 4. For the other player(s), think of another way to explain why the fraction is more or less and share with the group.
- 5. Pull another card and complete steps 2-4 until all cards have been used.

Round 3: Benchmark fraction $\frac{1}{3}$

- 1. Pull a card from the top of the stack.
- 2. Identify an equivalent fraction for the benchmark fraction.
- 3. Determine if the fraction is larger or smaller than $\frac{1}{3}$. Explain to your partner(s) why you believe it is greater than or less than using a number line.
- 4. For the other player(s), think of another way to explain why the fraction is more or less and share with the group.
- 5. Pull another card and complete steps 2-4 until all cards have been used.

Round 4:

- 1. Pull two cards from the top of the stack.
- 2. Determine which of the fractions is greatest. Explain to your partner(s) why you believe it is greater.
- 3. For the other player(s), think of another way to explain why the fraction is greater and share with the group.
- 4. Pull two more cards and complete steps 2-3 until all cards have been used.

FORMATIVE ASSESSMENT QUESTIONS

- Can you think of another way to explain the comparison?
- What equivalent fractions can you identify for _____?
- How do you know those fractions are equivalent?
- Which fraction is the least?
- Which fraction is greatest?

DIFFERENTIATION

Extension

• Have students work with fractions greater than 1, such as $\frac{5}{4}$ and $\frac{13}{12}$.

Intervention

• Allow students to use manipulatives to help compare the fractions.

• Encourage students to use number lines to compare the fractions. Intervention Table

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 42 of 90 All Rights Reserved

TECHNOLOGY

- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L541</u> More Fun with Fraction Strips: This lesson has students work with fraction strips to compare and order fractions using relationships. It can be used for additional practice, remediation or extending understanding of the concept.
- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L347</u> Exploring the Value of the Whole: This lesson has students consider the size or value of the same fraction when different wholes are compared. It can be used for remediation purposes, additional practice, and/or extending understanding of the concept.
- <u>https://www.conceptuamath.com/app/tool/comparing-fractions</u> *This online tool provides the opportunity for students to virtually compare fractions.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Name_

_____Date____

More or Less

Directions

Round 1: Benchmark fraction is $\frac{3}{4}$

- 1. Pull a card from the top of the stack.
- 2. Determine if the fraction is greater than or less than $\frac{3}{4}$. Using a number line, explain to your partner(s) why you believe it is greater than or less than $\frac{3}{4}$.
- 3. For the other player(s), think of another way to explain why the fraction is more or less and share with the group.
- 4. Pull another card and complete steps 2-3 until all cards have been used.

Round 2: Benchmark fraction $\frac{1}{2}$

- 1. Pull a card from the top of the stack.
- 2. Identify an equivalent fraction for the benchmark fraction.
- 3. Determine if the fraction is greater than or less than $\frac{1}{2}$. Using a number line, explain to your partner(s) why you believe it is greater than or less than $\frac{1}{2}$.
- 4. For the other player(s), think of another way to explain why the fraction is more or less and share with the group.
- 5. Pull another card and complete steps 2-4 until all cards have been used.

Round 3: Benchmark fraction $\frac{1}{3}$

- 1. Pull a card from the top of the stack.
- 2. Identify an equivalent fraction for the benchmark fraction.
- 3. Determine if the fraction is greater than or less than $\frac{1}{3}$. Using a number line, explain to your partner(s) why you believe it is greater than or less than $\frac{1}{3}$.
- 4. For the other player(s), think of another way to explain why the fraction is more or less and share with the group.
- 5. Pull another card and complete steps 2-4 until all cards have been used.

Round 4:

- 1. Pull two cards from the top of the stack.
- 2. Determine which of the fractions is greatest. Explain to your partner(s) why you believe it is greatest.
- 3. For the other player(s), think of another way to explain why the fraction is greater and share with the group.
- 4. Pull two more cards and complete steps 2-3 until all cards have been used.

Georgia Standards of Excellence Framework

GSE Fraction Equivalents \bullet Unit 3

More or Less Game Cards

| 6 | <u>3</u> | <u>5</u> |
|--------|----------|----------|
| 7 | 4 | 8 |
| 7 | <u>3</u> | 5 |
| 10 | 5 | 12 |
| 5 6 | 3 7 | 2 |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 45 of 90 All Rights Reserved

Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

| <u>3</u> 6 | <u> </u> | <u> 1 </u> |
|---------------|----------|--|
| <u> </u> | | 7 9 |
| <u>2</u> 4 | 2 6 | 3 8 |
| 4 5 | 1 1 | 4 4 |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 46 of 90 All Rights Reserved Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

<u>Practice Task:</u> Closest to $0, \frac{1}{2}$, or 1

Back to Task Table

Inspired by Math Solutions Publications Teaching Arithmetic: Lessons for Introducing Fractions by Marilyn Burns

TASK CONTENT: This task was developed to use as a continuation from the *Fraction Kits* task, but this is not a requirement. If students did not construct their own fraction kits, then they should be able to use other manipulatives that will enable them to have visual representations of equivalent fractions.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Constructing the idea that fractions are relationships and that the size or amount of the whole matters is a critical step in understanding fractions. Fair sharing contexts also provide learners with opportunities to explore how fractional parts can be equivalent without necessarily being congruent. They may look different but still be the same amount. Students have worked with the concept of fair share or partitioning since 2^{nd} grade, with standards that refer to same-sized shares or equal shares. Students should have knowledge of vocabulary terms such as numerator and denominator.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 47 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Some common misconceptions, found in *Math Misconceptions*, that children may include:

- Dividing nontraditional shapes into thirds, such as triangles, is the same as dividing a rectangle into thirds. If they are only used to dividing traditional shapes circles, squares, and rectangles they begin to think that all shapes are divided similarly.
- Children often do not recognize groups of objects as a whole unit. Instead they will incorrectly identify the objects. For example, there may be 2 cars and 4 trucks in a set of 6 vehicles. The student may mistakenly confuse the set of cars as 2/4 of the unit instead of 2/6 or 1/3 (Bamberger, Oberdorf, & Schultz-Ferrell, 2010).

Therefore, it is important that students are exposed to multiple units of measure, various shapes, and denominators other than halves, thirds, and fourths. Additionally, the denominator used as an expression of the whole is a key concept to express for mastery.

ESSENTIAL QUESTIONS

- How can equivalent fractions be identified?
- How can fractions be ordered on a number line?

MATERIALS

- Fraction kits constructed from Fraction Kits Task
- Number line
- Two number cubes (dice) per group

GROUPING

Small group or partner

NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" which may be included in a number talks to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents,* 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

Students can once again utilize the friendly number strategies to begin discussing multiples and specifically combining multiples to arrive at a larger product. For example, students could solve the following string of numbers:

 $1 \ge 12 = 12$ $2 \ge 12 = 24$

> Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 48 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

by combining the products of 12 and 24 as well as combining the factors of 1 and 2 the students will produce another multiple of 12, namely $3 \times 12 = 36$.

$$\begin{array}{r}
1 x 12 = 12 \\
+ 2 x 12 = 24 \\
\hline
3 x 12 = 36
\end{array}$$

Doubling and halving will also help students build equivalent fractions. (Number Talks, 2010, Sherry Parrish).

TASK DESCRIPTION, DEVELOPMENT, AND DISCUSSION

Comments

Students should have constructed their own fraction kit from the *Fraction Kits* task in this unit. It is important that you allow time for students to determine where each fraction should be placed on the number line. To enhance the understanding in this task, students may need to construct their own number lines from 0 to 1. This would also be an opportunity to review benchmark fractions by determining where they are placed on the number line. Students may need to stop to get fraction strips to check for equivalence. For students who are unable to determine the appropriate measures, ensure they are exposed to strategies discovered by their peers through classroom discussions.

This task was developed to use as a continuation from the *Fraction Kits* task, but this is not a requirement. If students did not construct their own fraction kits, then they should be able to use other manipulatives that will enable them to have visual representations of equivalent fractions.

Task Directions:

- The first player will roll the dice.
- The least number will represent the numerator while the greater number will be the denominator.
- Students will discuss if the fractions are closer 0, 1/2, or 1.
- Record the discussion result on the number line with a partner or group members. (Example: Write on the number line where $\frac{3}{4}$ would be located).
- Continue taking turns until each person has had a 10th turn.
- Once all turns have been taken, students should be able to accurately answer assessment questions.

FORMATIVE ASSESSMENT QUESTIONS

- Which fractions are close to $\frac{1}{2}$? What fractions are close to 1? Which fractions are close to 0?
- According to the fraction kit, which fraction is exactly the same as $\frac{2}{4}$?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 49 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

- How does the relationship between the denominator and the numerator change when it gets closer to $0, \frac{1}{2}$, or 1?
- What are some examples of equivalent fractions you identified during the game?

DIFFERENTIATION

Extension

Ask students to roll the dice twice for each turn. When they are rolled the first time, they should add the two dice, record it. They should roll them again and record the addition of the two dice again. The lesser number goes on the top and the greater number goes on the bottom. This allows for fractions beyond sixths. (i.e., ⁹/₁₂).

Intervention

• Have the students use the whole piece from the fraction kit as the number line. When they roll their fraction, for example $\frac{3}{4}$, they should collect the pieces from the fraction kit, line them up under the whole unit, and then record their fraction using this as a marker. This may have to be modeled before they work independently.

Intervention Table

TECHNOLOGY

- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L541</u> More Fun with Fraction Strips: This lesson has students work with fraction strips to compare and order fractions using relationships. It can be used for additional practice, remediation or extending understanding of the concept.
- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L347</u> Exploring the Value of the Whole: This lesson has students consider the size or value of the same fraction when different wholes compared. It can be used for remediation purposes, additional practice, and/or extending understanding of the concept.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Performance Task: Their Fair Share

Back to Task Table

Adapted from Fosnot, C. The Field Trip, Context for Learning Mathematics.

TASK CONTENT: In this task, students construct the idea that fractions are relationships and that the size or amount of the whole matters. The fair sharing context also provides learners with opportunities to explore how fractional parts can be equivalent without necessarily being congruent.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.MD.2 Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.

STANDARDS FOR MATHEMATICAL PRACTICES EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Constructing the idea that fractions are relationships and that the size or amount of the whole matters is a critical step in understanding fractions. Fair sharing contexts also provide learners with opportunities to explore how fractional parts can be equivalent without necessarily being congruent. They may look different but still be the same amount. Students have worked with the concept of fair share or partitioning since 2nd grade, with standards that refer to same-sized shares or equal shares.

ESSENTIAL QUESTIONS

- How can we use fair sharing to determine equivalent fractions?
- How do we know fractional parts are equivalent?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 51 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

MATERIALS

- Connecting cubes
- Equal length strips of paper/index cards
- Chart paper
- Fraction Kits from previous task (optional)

GROUPING

Small group or partner

NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" which may be included in a number talks to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents,* 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments

The numbers in this story have been chosen purposefully. Given the chosen numbers, students are catapulted into proportional reasoning. It is important that you facilitate discussions regarding their thinking at this point allowing them the opportunity to figure out how much each person in each group received.

When students begin to compare and/or add pieces together, some students may attempt to represent subs with the connecting cubes, but may not make equal size subs. If you see students using various sizes, be sure to point this out by asking if one group received bigger subs. Stay grounded in the context to help students realize the meaning of what they are doing. You want students to derive a common length sub in order to compare and/or add the fractional amounts. This idea is important for the construction of common denominators in fifth grade.

Make all materials available for use. Once students realize the need for a common length sub, you may offer them index cards to represent the subs. This becomes a powerful tool for understanding the fractional parts in relation to the same-sized whole.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 52 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Task directions:

Students will follow the directions below from the "Their Fair Share" student sheet.

A fourth grade class traveled on a field trip in four separate vehicles. The school provided a lunch of submarine sandwiches for each group. When they stopped for lunch, the one foot long subs were cut and shared as follows:

- The first group had 3 people and shared 2 subs equally.
- The second group had 4 people and shared 3 subs equally.
- The third group had 9 people and shared 6 subs equally.
- The last group had 6 people and shared 4 subs equally.

When they returned from the field trip, the children began to argue that the portion of the sandwiches they received was not fair and that some children got more to eat than others. Were they right or did everyone get the same amount?

Create a poster of the ideas and strategies you used to solve this problem. Be sure your poster is concise and clearly present the important ideas and strategies you want to present.

FORMATIVE ASSESSMENT QUESTIONS

- What initial cut did you make to your subs? Why?
- Did you use all parts of the subs? Were each of the parts equivalent?
- (For students using connecting cubes) Were all subs the same size? What amount of cubes could you use to show all of the subs were the same size?

DIFFERENTIATION

Extension

- Encourage students to try a different strategy to determine if they will arrive at the same fractional parts.
- Have students determine the length of each group's piece.

Intervention

- Have students use strips of equal length paper to represent the submarine sandwiches.
- Encourage students to use connecting cubes. Have them begin with 12 cubes to get them thinking about how to show common length subs.

Intervention Table

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 53 of 90 All Rights Reserved

Georgia Department of Education Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

TECHNOLOGY

- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L543</u> Investigating Equivalent Fractions with Relationship Rods: Students investigate the length model to find equivalent fractions in this lesson. It can be used for additional practice, remediation or extending understanding of the concept.
- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L338</u> Eggsactly Equivalent: This lesson involving finding equivalent fractions using eggs can be used for additional practice, remediation or extending understanding of the concept.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 54 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Name _____

Date

Their Fair Share Directions



A fourth grade class traveled on a field trip in four separate vehicles. The school provided a lunch of submarine sandwiches for each group. When they stopped for lunch, the one foot long subs were cut and shared as follows:

- The first group had 3 people and shared 2 subs equally.
- The second group had 4 people and shared 3 subs equally.
- The third group had 9 people and shared 6 subs equally.
- The last group had 6 people and shared 4 subs equally.

When they returned from the field trip, the children began to argue that the portion of the sandwiches they received was not fair and that some children got more to eat than others. Were they right or did everyone get the same amount?

Create a poster of the ideas and strategies you used to solve this problem. Be sure your poster is concise and clearly present the important ideas and strategies you want to present.

Georgia Department of Education Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

<u>3 ACT TASK:</u> Eating Cookies

<u>TASK CONTENT</u>: In this task, students will determine equivalent fractions of cookie pieces. Approximate time - 1 class period.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b}$ ex: $\frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

This task follows the 3-Act Math Task format originally developed by Dan Meyer. More information on this type of task may be found at <u>http://blog.mrmeyer.com/category/3acts/</u>. A Three-Act Task is a whole-group mathematics task consisting of 3 distinct parts: an engaging and perplexing Act One, an information and solution seeking Act Two, and a solution discussion and solution revealing Act Three. More information along with guidelines for 3-Act Tasks may be found in the *Guide to Three-Act Tasks* on georgiastandards.org.

Constructing the idea that fractions are relationships and that the size or amount of the whole matters is a critical step in understanding fractions. Fair sharing contexts also provide learners with opportunities to explore how fractional parts can be equivalent without necessarily being congruent. They may look different but still be the same amount. Students have worked

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 56 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

with the concept of fair share or partitioning from 2nd grade, with standards that refer to samesized shares or equal shares.

COMMON MISCONCEPTIONS

Some common misconceptions, found in *Math Misconceptions*, that children may experience include:

- Dividing nontraditional shapes into thirds, such as triangles, is the same as dividing a rectangle into thirds. If they are only used to dividing traditional shapes circles, squares, and rectangles they begin to think that all shapes are divided similarly.
- Children often do not recognize groups of objects as a whole unit. Instead they will incorrectly identify the objects. For example, there may be 2 cars and 4 trucks in a set of 6 vehicles. The student may mistakenly confuse the set of cars as 2/4 of the unit instead of 2/6 or 1/3 (Bamberger, Oberdorf, & Schultz-Ferrell, 2010).

Therefore, it is important that students are exposed to multiple units of measure, various shapes, and denominators other than halves, thirds, and fourths. Additionally, the denominator used as an expression of the whole is a key concept to express for mastery.

ESSENTIAL QUESTIONS

- How can equivalent fractions be identified?
- How can fractions be ordered on a number line?

MATERIALS

- 3 Act Task Student Recording Sheet
- Act 1 video <u>https://drive.google.com/file/d/17z6CBNXLfzOd9192snmTGq_yE_qcJBAv/view?usp=sh</u> <u>aring</u>
- Fraction circles
- Fraction outline

GROUPING

• Partners/small group

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

In this task, students will watch the video and then tell what they noticed. Next, they will be asked to discuss what they wonder about or are curious about. Their curiosities will be recorded as questions on a class chart or on the board. Students will then use mathematics to answer their

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 57 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

own questions. Students will be given information to solve the problem based on need. When they realize they don't have the information they need, and ask for it, it will be given to them. **Task Directions**

Act I – Whole Group - Pose the conflict and introduce students to the scenario by showing Act I video.

- 1. Show the Act I video to students. https://drive.google.com/file/d/0B0S_r7_2OlzNMGhFN0tYcEFFNDg/edit?usp=sharing
- 2. Pass out the 3 Act recording sheet.
- 3. Ask students what they wonder about and what questions they have about what they saw. Students should share with each other first before sharing aloud and then record these questions on the recording sheet (think-pair-share). The teacher may need to guide students so that the questions generated are math-related.

Anticipated questions students may ask and wish to answer:

How many pieces of cookies are there? What fraction of the 3 cookies was eaten? How could the remaining cookies be shared among the three girls? Which cookie, if shared, will yield the most cookie for each child? What fraction of the cookies did each girl eat? Were the cookies shared fairly among the three girls? ***Main question to answer.**

4. As the facilitator, you can select which question you would like every student to answer, have students vote on which question the class will answer or allow the students to pick which question they would like to answer. Once the question is selected ask students to estimate answers to their questions (think-pair-share). Students will write their best estimate, then write two more estimates – one that is too low and one that is too high so that they establish a range in which the solution should occur. Instruct students to record their estimates on a number line.

Act II – Student Exploration - Provide additional information as students work toward solutions to their questions.

- 1. Ask students to determine what additional information they will need to solve their questions. The teacher provides that information only when students ask for it.
 - All cookies were the same size.
 - Supply students with the cookie replicas.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

- 2. Ask students to work in small groups or with a partner to answer the questions they created in Act I. The teacher provides guidance as needed during this phase by asking questions such as:
 - Can you explain what you've done so far?
 - What strategies are you using?
 - What assumptions are you making?
 - What tools or models may help you?
 - Why is that true?
 - Does that make sense?

Act III - Whole Group - Share student solutions and strategies as well as Act III solution.

- 1. Ask students to present their solutions and strategies.
- 2. Compare solutions.
- 3. Lead discussion to compare these, asking questions such as:
 - How reasonable was your estimate?
 - Which strategy was most efficient?
 - Can you think of another method that might have worked?
 - What might you do differently next time?

Comments

Act IV is an extension question or situation of the above problem. An Act IV can be implemented with students who demonstrate understanding of the concepts covered in Acts II and III. The following questions and/or situations can be used as an Act IV:

• If 3 cookies is the whole, what fraction of cookie is left?

FORMATIVE ASSESSMENT QUESTIONS

- What models did you create?
- What organizational strategies did you use?

DIFFERENTIATION

Extension

- Have students complete Act 4.
- Students can investigate another question on the Act 1 list.

Intervention

• Allow students to use fraction circles to model the cookies in the problem.

Intervention Table

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 59 of 90 All Rights Reserved

TECHNOLOGY CONNECTIONS

- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L541</u> More Fun with Fraction Strips: This lesson has students work with fraction strips to compare and order fractions using relationships. It can be used for additional practice, remediation or extending understanding of the concept.
- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L347</u> Exploring the Value of the Whole: This lesson has students consider the size or value of the same fraction when different wholes are compared. It can be used for remediation purposes, additional practice, and/or extending understanding of the concept.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 60 of 90 All Rights Reserved

Georgia Department of Education Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

Act II Image – Cookie Replicas



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 61 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Name: _____

Adapted from Andrew Stadel

Task Title:

<u>ACT 1</u>

What questions come to your mind?

Main question:

On an empty number line, record an estimate that is too low, just right and an estimate that is too high. Explain your estimates.

<u>ACT 2</u>

What information would you like to know or need to solve the MAIN question?

Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

Use this area for your work, tables, calculations, sketches, and final solution.

<u>ACT 3</u>

What was the result?

Record the actual answer on the number line above containing the three previous estimates.

ACT 4 (use this space when necessary)

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 63 of 90 All Rights Reserved



<u>Practice Task:</u> Equivalent Fractions

Back to Task Table

Adapted from "Slicing Squares" from *Elementary and Middle School Mathematics: Teaching Developmentally* (6th ed.) by John Van de Walle

TASK CONTENT: This task allows students to explore the relationship between equivalent fractions and write equations for equivalent fractions using the product and quotient of a fraction equivalent to one.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE TO BE EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Constructing the idea that fractions are relations and that the size or amount is relative to the whole is a critical step in understanding fractions. Fair sharing contexts also provide learners with opportunities to explore how fractional parts can be equivalent without necessarily being congruent. They may look different but still be the same amount. Students have worked with the concept of fair share or partitioning since 2^{nd} grade, with standards that refer to same-sized

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 64 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

shares or equal shares. Students should have knowledge of vocabulary terms such as numerator and denominator.

Some common misconceptions, found in *Math Misconceptions*, that children have include:

- Dividing nontraditional shapes into thirds, such as triangles, is the same as dividing a rectangle into thirds. If they are only used to dividing traditional shapes circles, squares, and rectangles they begin to think that all shapes are divided similarly.
- Children often do not recognize groups of objects as a whole unit. Instead they will incorrectly identify the objects. For example, there may be 2 cars and 4 trucks in a set of 6 vehicles. The student may mistakenly confuse the set of cars as 2/4 of the unit instead of 2/6 or 1/3 (Bamberger, Oberdorf, & Schultz-Ferrell, 2010).

Therefore, it is important that students are exposed to multiple units of measure, various shapes, and denominators other than halves, thirds, and fourths. Additionally, the denominator used as an expression of the whole is a key concept to express for mastery.

ESSENTIAL QUESTIONS

- What happens to the value of a fraction when the numerator and denominator are multiplied or divided by the same number?
- How are equivalent fractions related?

MATERIALS

- "Equivalent Fractions, $\frac{2}{3}$ " student recording sheet
- "Equivalent Fractions, $\frac{3}{4}$ ", student recording sheet

GROUPING

Individual or partner

NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" that could be included in a number talk to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents,* 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 65 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Students can utilize the friendly number strategies to begin discussing multiples and specifically combining multiples to arrive at a larger product. For example, students could solve the following string of numbers:

1 x 12 = 122 x 12 = 24by combining the products of 12 and 24 as well as combining the factors of 1 and 2 the students will produce another multiple of 12, namely 3 x 12 = 36

 $\begin{array}{r}
1 x 12 = 12 \\
+ 2 x 12 = 24 \\
\hline
3 x 12 = 36
\end{array}$

Doubling and halving is also a helpful strategy in building equivalent fractions. (Number Talks, 2010, Sherry Parrish).

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Task Directions

Students will follow the directions below from the "Equivalent Fractions $-\frac{2}{3}$ " student recording sheet.

Find fractions that are equivalent to the fraction shown in each square below. Slice the squares by drawing horizontal line segments in each square to create a different but equivalent fraction. Then write an equation for each model. See the example below.



Students will follow the directions below from the "Equivalent Fractions $-\frac{3}{4}$ " student recording sheet.

Find fractions that are equivalent to the fraction shown in each square below. Slice the squares by drawing horizontal line segments in each square to create a different but equivalent fraction. Then write an equation for each square.

Comments

This task allows students to explore the relationship between equivalent fractions and write equations for equivalent fractions using the product and quotient of a fraction equivalent to one.

This task is adapted from Van De Walle, J. (2007). *Elementary and Middle School Mathematics: Teaching Developmentally* (6th ed.) Boston: Pearson Education, Inc. See the section on "Equivalent Fraction Concepts." (This task is adapted from an activity titled "Slicing Squares" on p. 311.)

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 66 of 90 All Rights Reserved

Georgia Department of Education Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Give students the opportunity to explore equivalent fractions with this task. Encourage students to look for patterns, both in the models as well as in the numerical representations. Equivalent fractions can be thought of as different names for a fraction.

Once students have written equivalent fractions and are able to show that the fraction was multiplied by a fraction equivalent to 1, then begin the discussion about using the inverse operation. Ask students how they can simplify a fraction by dividing it by a fraction equivalent to 1. See the examples below.

$$\frac{2}{3} = \frac{2}{3} \times \frac{4}{4} = \frac{8}{12}; \frac{8}{12} = \frac{8}{12} \div \frac{4}{4} = \frac{2}{3} \qquad \qquad \frac{3}{4} = \frac{3}{4} \times \frac{2}{2} = \frac{6}{8}; \frac{6}{8} = \frac{6}{8} \div \frac{2}{2} = \frac{3}{4}$$

Possible solutions to the "Equivalent Fractions - $\frac{2}{3}$ " student recording sheet are shown below:



Possible solutions to the "Equivalent Fractions - $\frac{3}{4}$ ", student recording sheet are shown below.



FORMATIVE ASSESSMENT QUESTIONS

- Into how many parts did you slice each piece?
- What is a fraction that is equivalent to one? (If the student sliced each piece into three parts, they need to multiply the fraction by $\frac{3}{3}$.)
- How could you use equivalent fractions to simplify this fraction (i.e. $\frac{6}{2}$)?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 67 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

- What is the same about all of the models? (The amount of space shaded in has stayed the same.)
- What is different about the models? (The size of the pieces have gotten smaller, so there are more pieces.)

DIFFERENTIATION

Extension

• Invite students to play the Fraction Game. <u>http://illuminations.nctm.org/ActivityDetail.aspx?ID=18</u> This game requires students to recognize equivalent fractions. Students should think about scenarios from the game that could be presented to the class so that students can discuss strategies and choices available to them.

Intervention

- Some students may benefit from having a table of equivalent fractions. Ask students to complete the table by multiplying the numerator and denominator by the same number.
- <u>*Intervention Table</u>

TECHNOLOGY CONNECTION

- <u>https://prod.classflow.com/classflow/#!/product/itemId=91d03de3f5e14311b07ed97489e</u> <u>e87d4</u> This lesson can be used with an ActivSlate or Smartboard. It can be used as a mini-lesson to introduce the task or for remediation purposes.
- <u>https://learnzillion.com/lesson_plans/567-examine-patterns-that-occur-when-you-multiply-or-divide-both-the-numerator-and-denominator-by-the-same-number</u> LearnZillion – Examine Patterns that occur when you multiply or divided both the numerator and the denominator by the same number: This LearnZillion lesson plan has discusses the patterns and models shown in this lesson. This lesson could be used for remediation if students need another go at the concept.

<u>https://www.conceptuamath.com/app/tool/equivalent-fractions</u> This online tool provides students with the opportunity to virtually manipulate fraction circles, fraction bars, and number lines to explore equivalent fractions.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3



Equivalent Fractions $-\frac{2}{3}$

Find fractions that are equivalent to the fraction shown in each square below. Slice the squares by drawing horizontal line segments in each square to create a different but equivalent fraction. Then write an equation for each square. See the example below.



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 69 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3



Equivalent Fractions $-\frac{3}{4}$

Find fractions that are equivalent to the fraction shown in each square below. Slice the squares by drawing horizontal line segments in each square to create a different but equivalent fraction. Then write an equation for each square.



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 70 of 90 All Rights Reserved

Georgia Department of Education Georgia Standards of Excellence Framework ~~~ **-**Faring1

| GSE Fraction Equivalents \bullet Unit 3 | | | | | | | | | |
|--|----------------|--|--|--|--|---------------|--|--|--|
| Name | Jame Date | | | | | | | | |
| Equivalent Fractions Find fractions equivalent to the fractions in the table below. Record the equivalent fractions in the white boxes. $\begin{array}{c} 2 \\ 6 \\ 3 \end{array}$ | | | | | | | | | |
| $\frac{1}{2}$ | | | | | | $\frac{3}{4}$ | | | |
| $\frac{1}{3}$ | | | | | | $\frac{2}{5}$ | | | |
| $\frac{1}{4}$ | | | | | | $\frac{3}{5}$ | | | |
| $\frac{1}{5}$ | | | | | | $\frac{4}{5}$ | | | |
| $\frac{1}{6}$ | $\frac{2}{12}$ | | | | | $\frac{4}{6}$ | | | |
| $\frac{2}{3}$ | | | | | | <u>5</u> 6 | | | |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 71 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Practice Task: Making Fractions

Back to Task Table

Adapted from Actions on Fractions, Navigating through Number and Operations in Grades3-5.

TASK CONTENT: Students play a game to practice comparing fractions.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.

BACKGROUND KNOWLEDGE

Students were familiarized with benchmark fractions in 2^{nd} grade. They worked to partition circles and rectangles into halves and thirds. In 3^{rd} grade students generated simple equivalent fractions and were required to explain why the fractions were equivalent.

ESSENTIAL QUESTIONS

- How can you compare and order fractions?
- How are benchmark fractions helpful when comparing fractions?
- How do I compare fractions with unlike denominators?

MATERIALS

• Playing cards with all face cards removed

GROUPING

Partners

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 72 of 90 All Rights Reserved
NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. In addition, Catherine Fosnot has developed problem "strings" which may be included in number talks to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents*, 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments: Students should follow the rules discussed on the "Making Fractions" student sheet.

How to Play:

- A player deals four cards to themselves and four to their partner.
- Both players make the greatest fraction that they can by choosing a numerator and a denominator from the numbers on their cards.
- Compare your fractions. The one with the greatest fraction wins all the cards and becomes the new dealer for the next round.
- If the fractions are equal, the round ends in a tie, and the players keep their cards.
- The game continues in this manner until the players have used all cards.
- Each player counts their cards and the one with more cards wins.

FORMATIVE ASSESSMENT QUESTIONS

- Can you think of another way to explain the comparison?
- What equivalent fractions can you identify for _____
- How do you know those fractions are equivalent?
- Which fraction is the least?
- Which fraction is the greatest?

DIFFERENTIATION

Extension

- Change the rules of the game by having players create the fraction that is worth the least.
- Increase the group size to require students to compare and order more than two fractions.
- Instruct students to only use proper fractions.
- Students can roll a die or spin a spinner to determine the winner for each round. If an odd digit is rolled or spun, the greatest fraction wins. If an even digit is rolled or spun, the fraction that is the least wins.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 73 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Intervention

- Allow students to create their fractions using manipulatives.
- Encourage students to use benchmark fractions to help compare created fractions.
- Encourage students to compare fractions created on number lines.

Intervention Table

TECHNOLOGY

- <u>https://prod.classflow.com/classflow/#!/product/itemId=91d03de3f5e14311b07ed97489e</u> <u>e87d4</u> This lesson can be used with an ActivSlate or Smartboard. It can be used as a mini-lesson to introduce the task or for remediation purposes.
- <u>https://learnzillion.com/lesson_plans/562-compare-two-fractions-with-different-numerators-and-denominators-by-using-linear-models</u> LearnZillion Lesson Plan Compare two fractions with different numerators and denominators by using linear models: This LearnZillion lesson plan discusses how to use number lines to compare fractions with different numerators and denominators.

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 74 of 90 All Rights Reserved

Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

Name _____ Date _____

Making Fractions Directions

How to Play:

- A player deals four cards to themselves and four to their partner.
- Both players make the greatest fraction that they can by choosing a numerator and a denominator from the numbers on their cards.
- Compare your fractions. The one with the greatest fraction wins all the cards and becomes the new dealer for the next round.
- If the fractions are equal, the round ends in a tie, and the players keep their cards.
- The game continues in this manner until the players have used all cards.
- Each player counts their cards and the one with more cards wins.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Performance Task: Write About Fractions

Back to Task Table

Adapted from Fosnot, C. The Field Trip, Context for Learning Mathematics.

TASK CONTENT: In this task, students construct a viable argument based on their understanding of equivalent fractions and their knowledge of strategies that are useful when comparing fractions with different denominators.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE TO BE EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

BACKGROUND KNOWLEDGE

Many students develop misconceptions about adding fractions, thinking the numerators can be added and denominators can be added. Students need to assess the reasonableness of their results when thinking about adding and subtracting fractions. This involves thinking about fractions as quantities instead of viewing them as two separate numbers, a numerator and a denominator.

ESSENTIAL QUESTIONS

- How can comparing fractions help make sense of adding fractions?
- How do you know fractions are equivalent?
- What can you do to decide whether your answer is reasonable?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 76 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

MATERIALS

- Connecting cubes
- Strips of equal length paper
- Write About Fractions task sheet
- Fraction Kits

GROUPING

Individual

NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" which may be included in the Number Talks session to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents*, 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments

Students have had some opportunities to work with comparing unit fractions with different denominators in context. Exploring this procedure in context and examining the results supports students to develop deep understandings about fractions, thereby avoiding common misconceptions.

Task directions:

Students will follow the directions below from the "Write About Fractions" task sheet.

Write a convincing argument for the following statement:

 $\frac{1}{2} + \frac{1}{3}$ does not equal $\frac{2}{5}$

FORMATIVE ASSESSMENT QUESTIONS

- What do you notice about the unit fractions you have created?
- How can drawing a model help you answer this question?
- What strategies can you use to help write about this topic?
- Can you give me an estimated size of the fraction you created with that cut?
- Does your answer make sense? How do you know?

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 77 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

DIFFERENTIATION

Extension

• In addition to this task, student can identify a fraction that is equal to $\frac{1}{2} + \frac{1}{3}$.

Intervention

- Provide fraction strips the students can manipulate to determine their response.
- Encourage students to use words, numbers and/or pictures in their explanation.

Intervention Table

TECHNOLOGY

- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L543</u> This lesson has students investigate the length model to find equivalent fractions. It can be used for additional practice, remediation or extending understanding of the concept.
- <u>http://illuminations.nctm.org/LessonDetail.aspx?ID=L338</u> This lesson involving finding equivalent fractions using eggs can be used for additional practice, remediation or extending understanding of the concept.

Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3

| Name | |
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Date

Write About Fractions

Write a convincing argument for the following statement:

 $\frac{1}{2} + \frac{1}{3}$ does not equal $\frac{2}{5}$

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 79 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Culminating Task: Pattern Block Puzzles Revisited

Back to Task Table

TASK CONTENT: For this activity students are asked to cover up shapes that were made with pattern blocks. The shapes are "grayed out" so students will be forced to determine how best to cover them.

STANDARDS FOR MATHEMATICAL CONTENT

MGSE4.NF.1 Explain why two or more fractions are equivalent $\frac{a}{b} = \frac{n \times a}{n \times b} \operatorname{ex}: \frac{1}{4} = \frac{3 \times 1}{3 \times 4}$ by using visual fraction models. Focus attention on how the number and size of the parts differ even though the fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

MGSE4.NF.2 Compare two fractions with different numerators and different denominators, e.g., by using visual fraction models, by creating common denominators or numerators, or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions.

STANDARDS FOR MATHEMATICAL PRACTICE TO BE EMPHASIZED

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning

BACKGROUND KNOWLEDGE

Encourage students to organize their thinking to be sure they have found as many ways as possible to represent equivalent fractions. Possible equivalent fractions are shown below. Before asking students to work on this task, be sure students are able to:

- recognize how pattern blocks can represent fractions
- find equivalent fractions for pattern blocks if a hexagon is assigned the value of one whole
- write an equation which shows the equivalent fractions
- identify where a fraction would be found on a number line
- understand that fractions are a quantity that can be greater than or less than the value of one whole

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 80 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

ESSENTIAL QUESTIONS

- How can we find equivalent fractions?
- In what ways can we model equivalent fractions?
- How can identifying factors and multiples of denominators help to identify equivalent fractions?
- How do we represent a fraction that is greater than one?
- How do we locate fractions on a number line?

MATERIALS

- Pattern blocks
- "Pattern Block Puzzles" student recording sheet
- Die cut pattern blocks or pencils and crayons for recording findings
- Isometric graph paper

GROUPING

Individual or partner

NUMBER TALKS

Continue utilizing the different strategies in number talks and revisiting them based on the needs of your students. Catherine Fosnot has developed problem "strings" that could be included in a number talk to further develop mental math skills. See *Mini-lessons for Operations with Fractions, Decimals, and Percents* by Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard. (*Mini-lessons for Operations with Fraction, Decimal, and Percents*, 2007, Kara Louise Imm, Catherine Twomey Fosnot and Willem Uittenbogaard)

Students can utilize the friendly number strategies to begin discussing multiples and specifically combining multiples to arrive at a larger product. For example, students could solve the following string of numbers:

 $1 \ge 12 = 12$ $2 \ge 12 = 24$

By combining the products of 12 and 24 as well as combining the factors of 1 and 2 the students will produce another multiple of 12, namely $3 \times 12 = 36$

 $\begin{array}{r}
1 x 12 = 12 \\
+ 2 x 12 = 24 \\
\hline
3 x 12 = 36
\end{array}$

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 81 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Doubling and halving is also a helpful strategy in building equivalent fractions. (Number Talks, 2010, Sherry Parrish).

TASK DESCRIPTION, DEVELOPMENT AND DISCUSSION

Comments

For this activity students are asked to cover shapes that were made with pattern blocks. The shapes are "grayed out" so students will be forced to determine how best to cover them. There are several ways to accomplish each puzzle. The first puzzle is a larger hexagon and it is possible to cover this shape with all trapezoids, all rhombi, all triangles or a combination of trapezoid, rhombi, triangles and hexagons. Through discovery students will realize that hexagons alone will not cover up the larger hexagon puzzle. The second puzzle can be covered up by all trapezoids, all triangles or a combination of hexagons, trapezoids, rhombi and triangles. The final puzzle can be covered up with all rhombi or all triangles or a combination of hexagons, trapezoids, rhombi and triangles.

As a mini lesson, introduce the yellow hexagon and have students explore all the other ways you can make a hexagon. Through this activity students will discover that a hexagon can be made with a combination of other pattern blocks or it can be made with 2 trapezoids, 3 rhombi or 6 triangles. Through discussion the class can now assign a value to all the pattern blocks in relation to the hexagon, namely a trapezoid = $\frac{1}{2}$, a rhombus = $\frac{1}{3}$, and a triangle = $\frac{1}{6}$. In many ways this task is similar to the "Who Put the Tang in Tangram" task. However, that task only allowed students to work with the fraction $\frac{1}{2}$ to explore repeated addition and multiplication of fractions, this activity allows students to continue exploring operations with fractions while also finding equivalent fractions, as well as creating their own puzzles!

Task Directions:

Cover the shape below with pattern blocks any way you'd like.

Now cover the shape using only one color of pattern blocks. Record your information below: If a hexagon has a value of one whole, what is the value of the pattern block you chose?

How many pattern blocks did you use to cover this shape? ______ Write the area of the shape below as a fraction of a hexagon. ______ What is another way you could cover this shape using only one color of pattern blocks? If a hexagon has a value of one whole, what is the value of the pattern block you chose? ______ How many pattern blocks did you use to cover this shape? ______

| Write the | area of the sl | hape below as a | a fraction of a h | exagon. | | | |
|--------------|----------------|-----------------|-------------------|---------|---|---|---------------|
| Locate th | at fraction on | the number lin | e below: | | | | |
| \leftarrow | | | | | | | \rightarrow |
| | | | | | | | |
| | 0 | 1 | 2 | 3 | 4 | 5 | |

Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 82 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

FORMATIVE ASSESSMENT QUESTIONS

- How are you keeping your work organized?
- Have you found all the possible ways to cover each puzzle?
- What is another way to cover the puzzle?
- How do you know these two fractions are equivalent?
- How many triangles cover up a hexagon, a rhombus, a trapezoid?
- Do any shapes seem to work with all puzzles?
- Do some shapes not work with certain puzzles? If so, why?
- Where would that fraction be on a number line?
- How did you find a second solution for each situation?
- Look at the posted solutions. Are there any that you think are not correct? If so, tell why.
- Do you think that there are other solutions beyond those posted? Explain.
- How is it possible that there could be more than one solution for each situation?

DIFFERENTIATION

Extension

- You can introduce the idea that the value of one can always change, such as 1 dozen doughnuts or eggs can be another way to think of a whole. Students can put two hexagons together and consider this their new whole. This will then change the value of all the shapes, namely a hexagon $= \frac{1}{2}$, a trapezoid $= \frac{1}{4}$, and a rhombus $= \frac{1}{6}$, and a triangle would equal $\frac{1}{12}$. Students could then solve each puzzle again and see if they can find a pattern between their previous solutions and their new ones.
- Students could exchange puzzles they created and solve one another's puzzle.
- Students could outline just the perimeter of a puzzle they created and challenge classmates to solve it and find equivalent fractions as well as area.
- Students could also make very large rectangle puzzles and begin to find the patterns that exist between fractions greater than one and mixed numbers.

Intervention

- Allow students to record equivalent fractions using pre-cut pattern blocks.
- Allow students to utilize isometric graph paper or dot paper to see the relationships that exist between the various pattern blocks. Students may even need to color them and use this as a key.

Intervention Table

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3



TECHNOLOGY

- There are several websites that offer virtual pattern blocks such as http://illuminations.nctm.org/ActivityDetail.aspx?ID=27
- <u>http://www.mathlearningcenter.org/web-apps/pattern-shapes/</u> *This tool provides the opportunity for students to virtually manipulate pattern blocks.

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Pattern Block Puzzles

Cover the shape below with pattern blocks any way you'd like. Now cover the shape using only one color of pattern blocks. Record your information below.

If a hexagon has a value of one whole, what is the value of the pattern block you chose?

How many pattern blocks did you use to cover this shape?

Write the area of the shape below as a fraction of a hexagon.

What is another way you could cover this shape using only one color of pattern blocks?

If a hexagon has a value of one whole, what is the value of the pattern block you chose?

How many pattern blocks did you use to cover this shape?

Write the area of the shape below as a fraction of a hexagon.

Locate that fraction on the number line below:



Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Cover the shape below with pattern blocks any way you'd like. Now cover the shape using only one color of pattern blocks. Record your information below. If a hexagon has a value of one whole, what is the value of the pattern block you chose? How many pattern blocks did you use to cover this shape? Write the area of the shape below as a fraction of a hexagon. Is there another way you could cover this shape using only one color of pattern blocks? If a hexagon has a value of one whole, what is the value of the pattern block you chose? How many pattern blocks did you use to cover this shape? Write the area of the shape below as a fraction of a hexagon. Locate that fraction on the number line below: \rightarrow 0 1 2 3 4 5



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 86 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

Create your own shape below with pattern blocks.

Now cover the shape using only one color of pattern blocks. Record your information below:

If a hexagon has a value of one whole, what is the value of the pattern block you chose?

How many pattern blocks did you use to cover this shape?

Write the area of the shape below as a fraction of a hexagon.

Is there another way you could cover your shape using only one color of pattern blocks?

If a hexagon has a value of one whole, what is the value of the pattern block you chose?

How many pattern blocks did you use to cover this shape?

Write the area of the shape below as a fraction of a hexagon.

Locate that fraction on the number line below:





Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 87 of 90 All Rights Reserved

Georgia Standards of Excellence Framework GSE Fraction Equivalents • Unit 3

PART 2

Create your own shape below with pattern blocks.

Now cover the shape using only one color of pattern blocks. Record your information below:

If a hexagon has a value of one whole, what is the value of the pattern block you chose?

How many pattern blocks did you use to cover this shape?

Write the area of the shape below as a fraction of a hexagon.

Is there another way you could cover your shape using only one color of pattern blocks?

If a hexagon has a value of one whole, what is the value of the pattern block you chose?

How many pattern blocks did you use to cover this shape?

Write the area of the shape below as a fraction of a hexagon.

Locate that fraction on the number line below:

| < | | | + | - | - | \rightarrow |
|---|---|---|---|---|---|---------------|
| | 0 | 1 | 2 | 3 | 4 | 5 |

Georgia Department of Education Georgia Standards of Excellence Framework

GSE Fraction Equivalents • Unit 3



Mathematics • GSE Grade 4• Unit 3: Fraction Equivalents Richard Woods, State School Superintendent July 2021 • Page 89 of 90 All Rights Reserved

Georgia Standards of Excellence Framework

GSE Fraction Equivalents \bullet Unit 3

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